

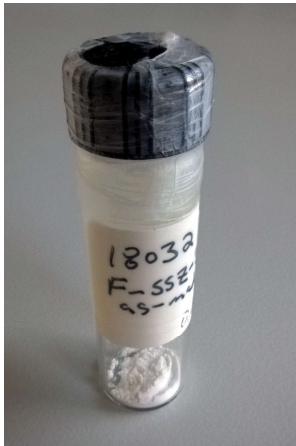
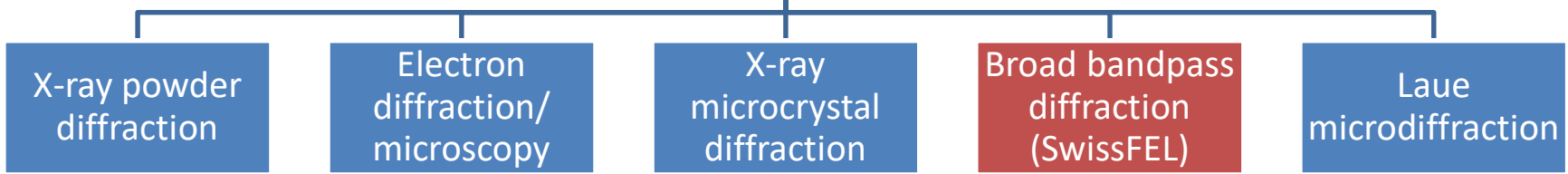
ECM 29, Rovinj, HR  
26-08-2015

**ETH** zürich

# INDEXING OF MULTI-CRYSTAL SNAPSHOTS COLLECTED WITH A BROAD BANDPASS BEAM

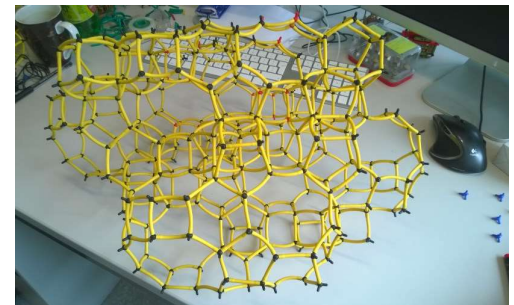
Stef Smeets  
Laboratory for Crystallography  
ETH Zurich, Switzerland

Polycrystalline material



Sample

???



Model

# SwissFEL (2017)

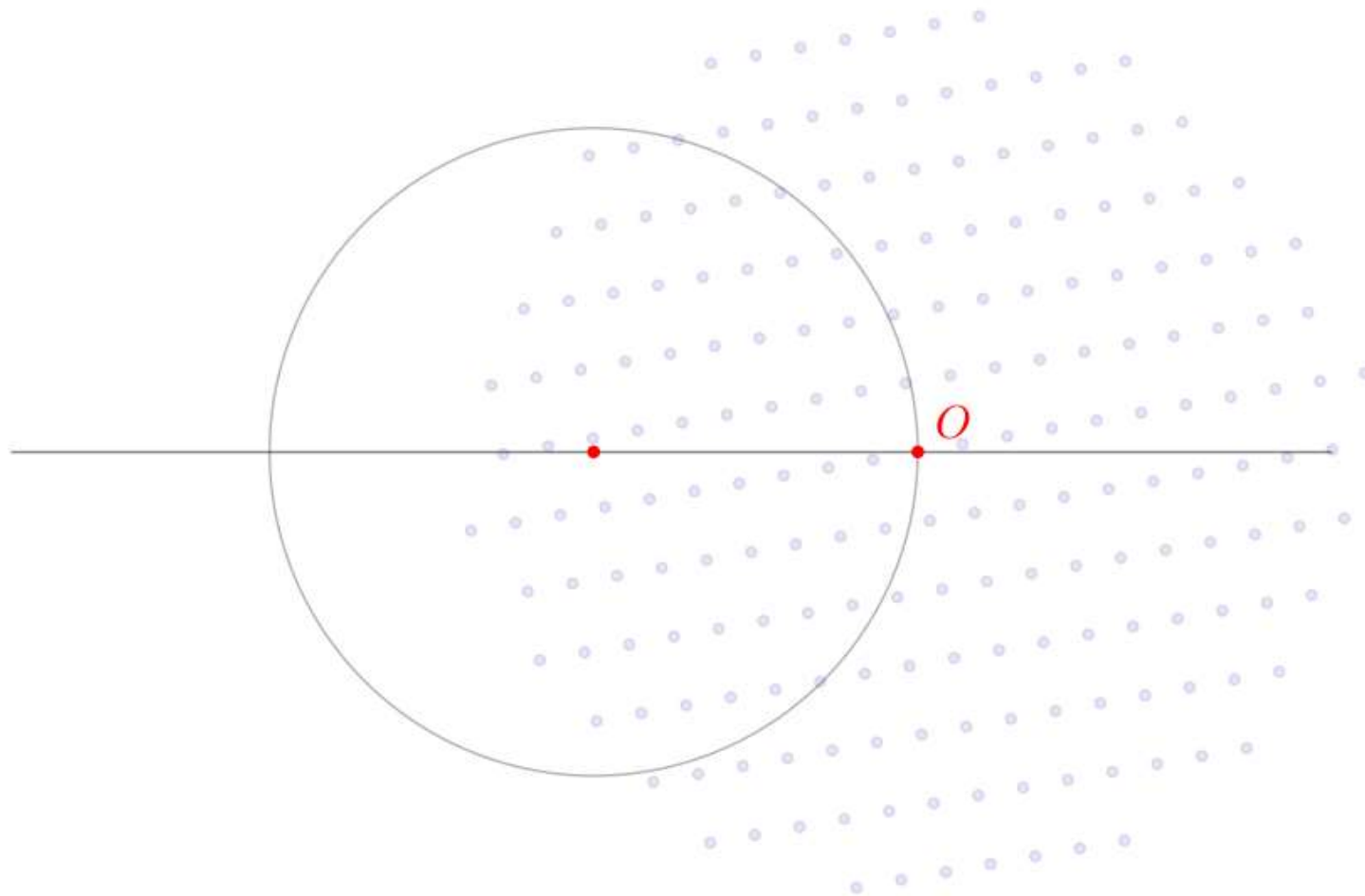
## Free electron laser

- Ultrashort, coherent X-ray pulses
- High brilliance
- Broad bandpass beam mode (4%; SwissFEL only)

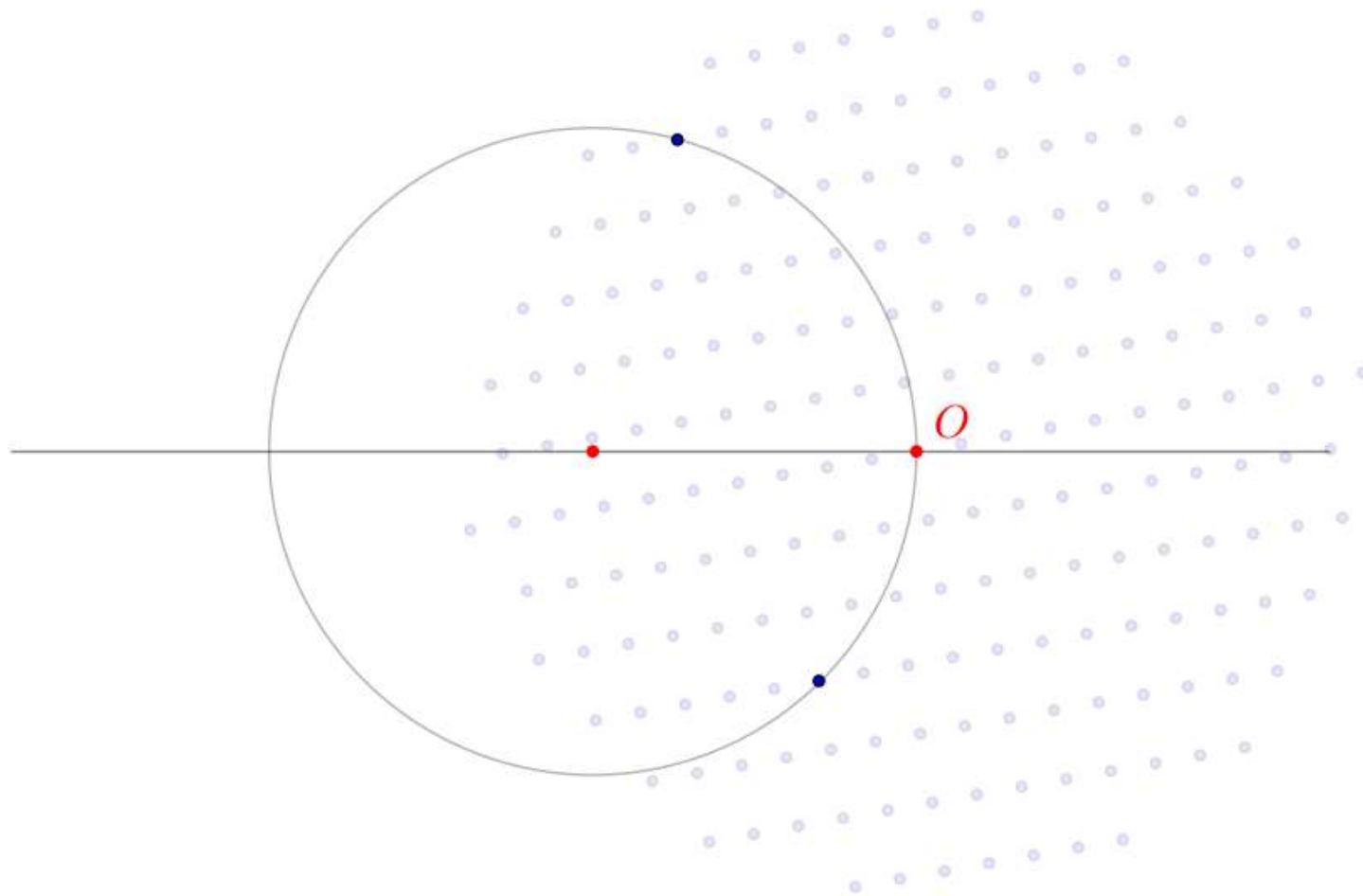
## Develop methodology to use this mode for structure solution

- Serial snapshot crystallography
- Organic/Inorganic materials
- 'small unit cell' ( $<25000 \text{ \AA}^3$ )
- Multiple crystals

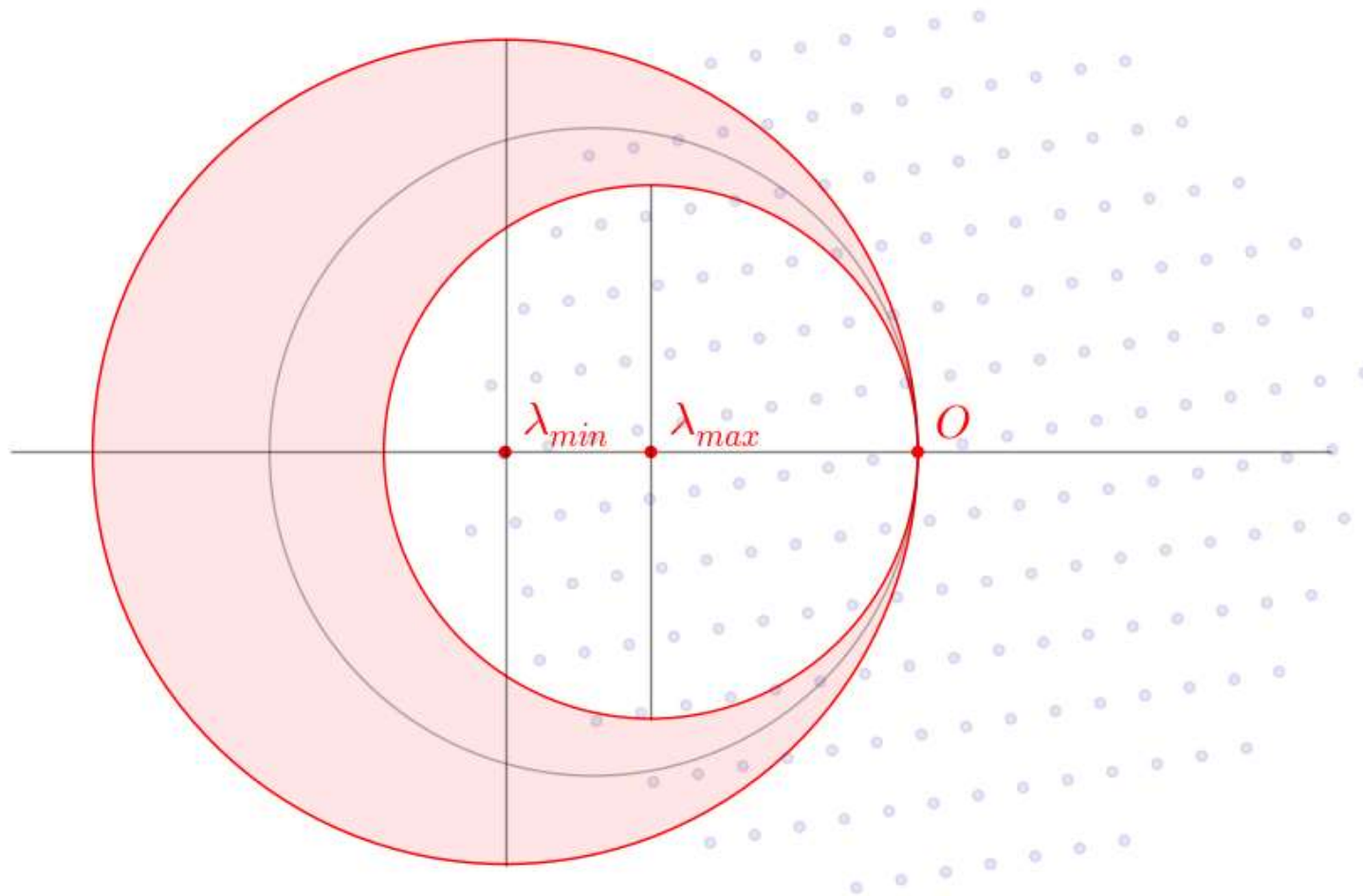
*C. Dejoie: Serial snapshot  
crystallography for materials science  
with SwissFEL (MS-13)*



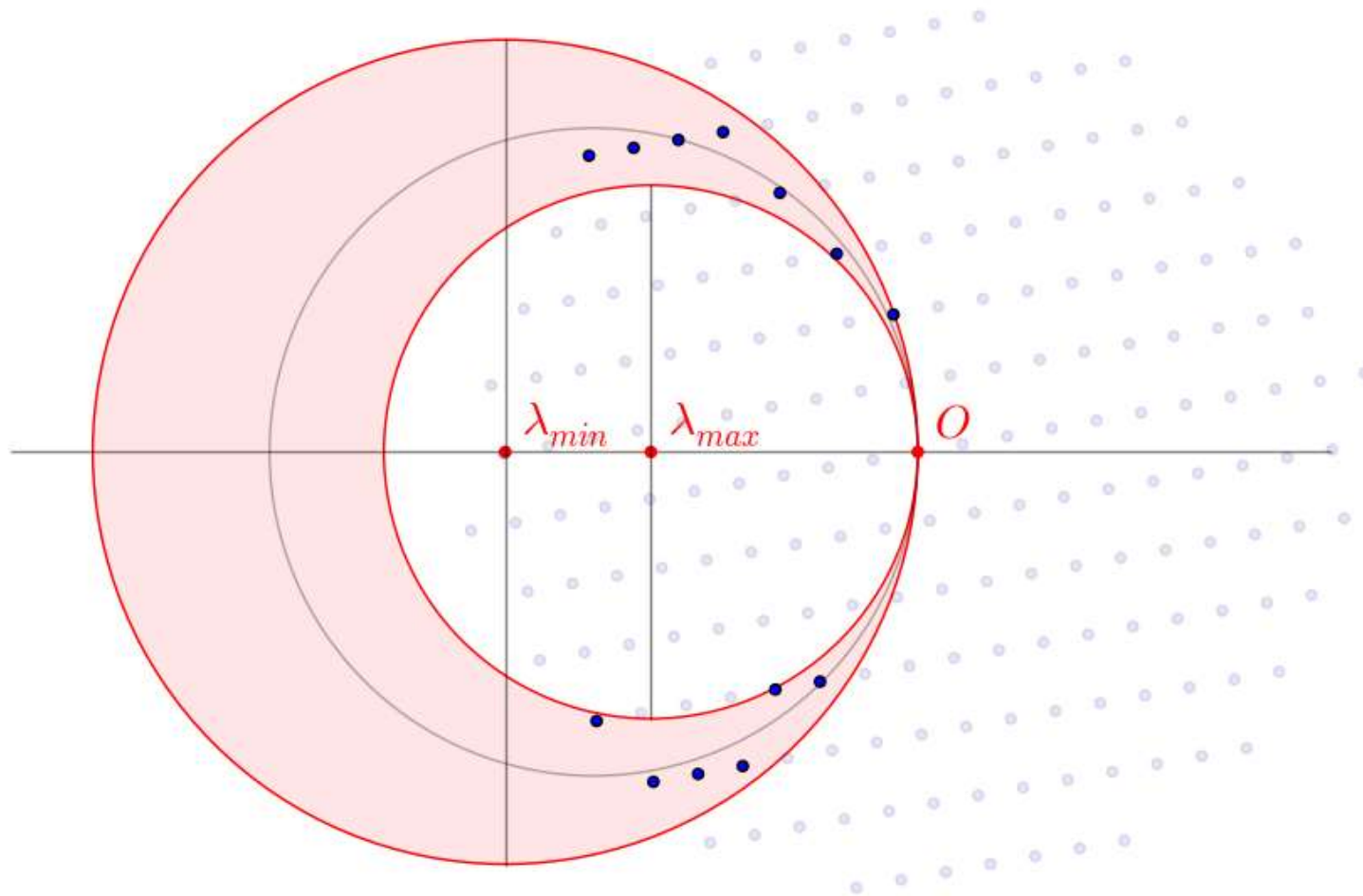
Single crystal (monochromatic radiation)



Single crystal (monochromatic radiation)

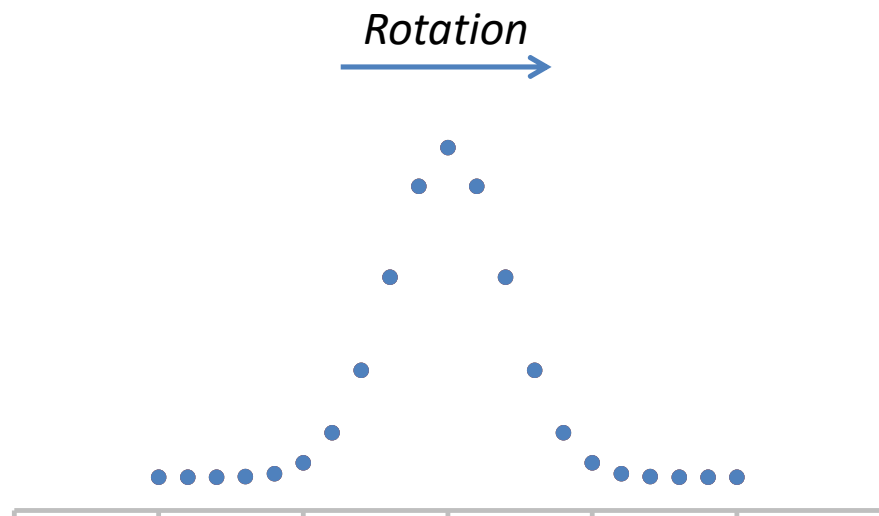


Single crystal (4% bandwidth)



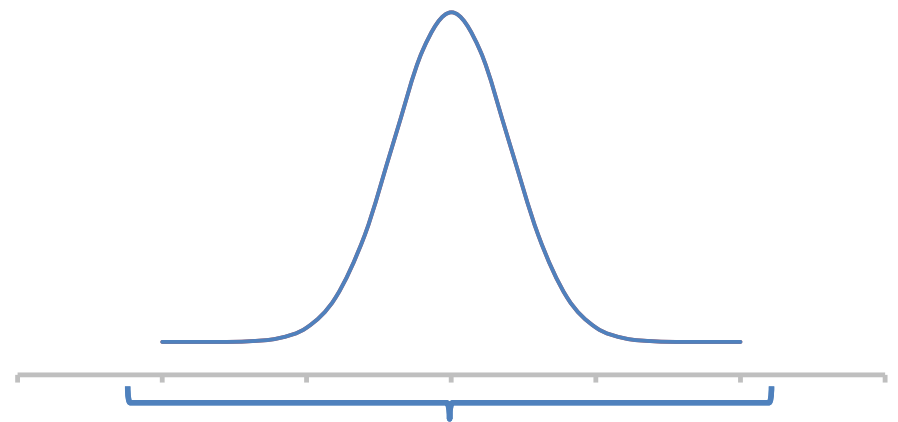
Single crystal (4% bandwidth)

# 4% bandwidth



Monochromatic

Rotating crystal  
Multiple shots



4% broadband

Stationary  
Single shot



# How to index the data?

## Four challenges

- 4% bandwidth
    - energy indeterminate
  - Single snapshot
  - Multiple crystals
  - Small unit cells
    - limited number of reflections
- Laue-based approach
    - *X-MAS* (N. Tamura, C. Dejoie)
  - Monochromatic approach
    - *DIRAX* (Duisenberg, 1992)
    - *DENZO* (Steller, 1997)
    - *XDS* (Kabsch, 1993)
    - *Cctbx.xfel*
    - *CrystFEL*

➤ Develop new indexing approach

Unit cell known  
Start with  $\mathbf{q}$ -vectors  
Assume average wavelength ( $\pm 2\%$ )

# Approach to indexing

## Generation

Generate candidate  
orientation matrices

1. Orientation matrix search  
Map  $d$ -spacings to potential indices  
Use peak pairs

## Evaluation

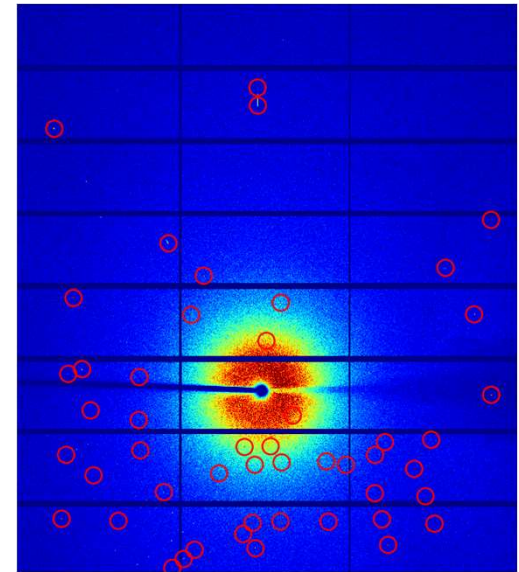
Select good candidate(s)  
(number of indexed peaks  $N_{fit}$ )

Assign wavelength & calculate *score*  
Ranked by  $score/N_{fit}^2$


Greedy set optimization routine  
(Multiple crystals only)

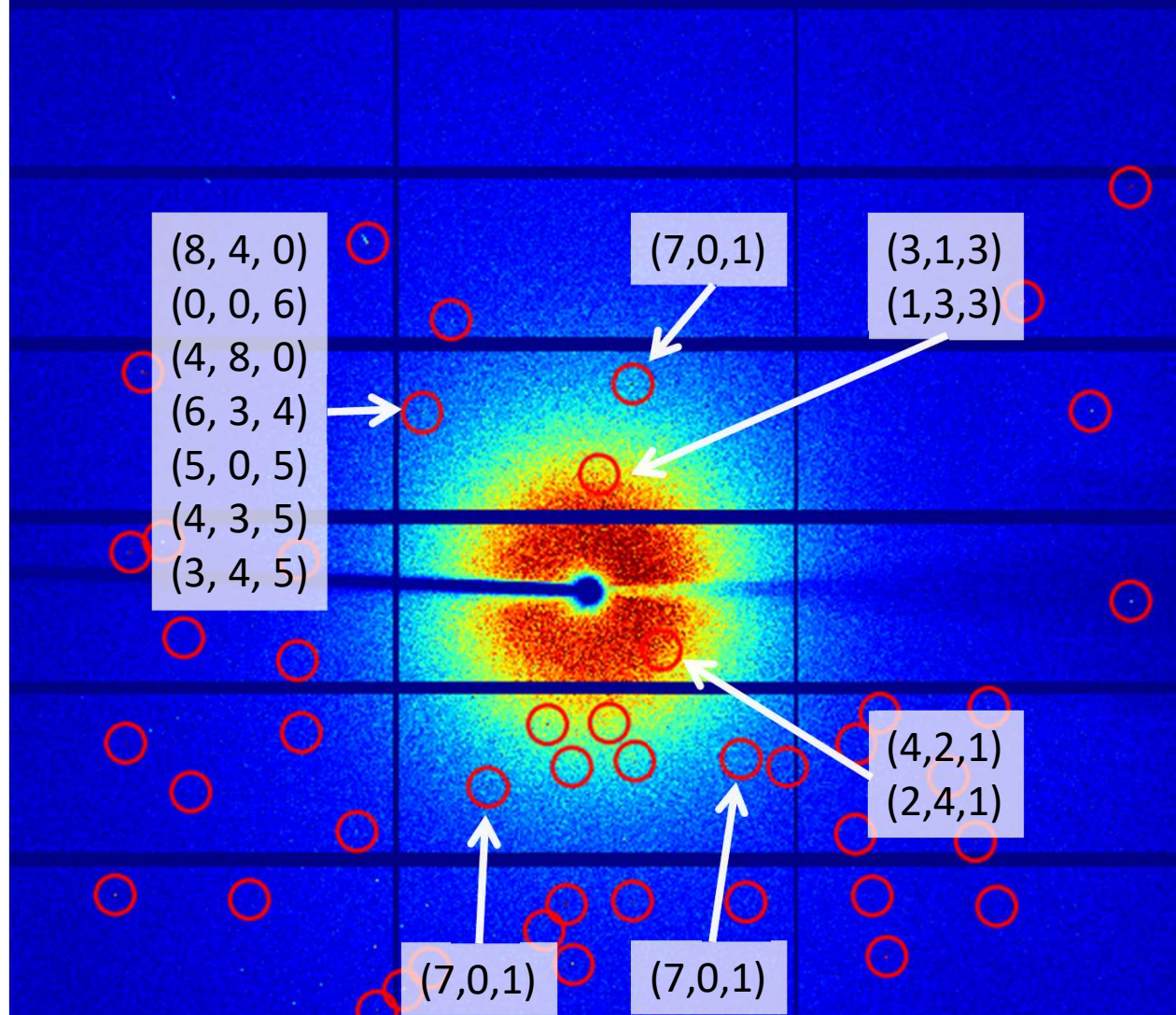
# Typical run (ZSM-5)

- 58 peaks in frame, take 10 peaks with lowest  $2\theta$  angle



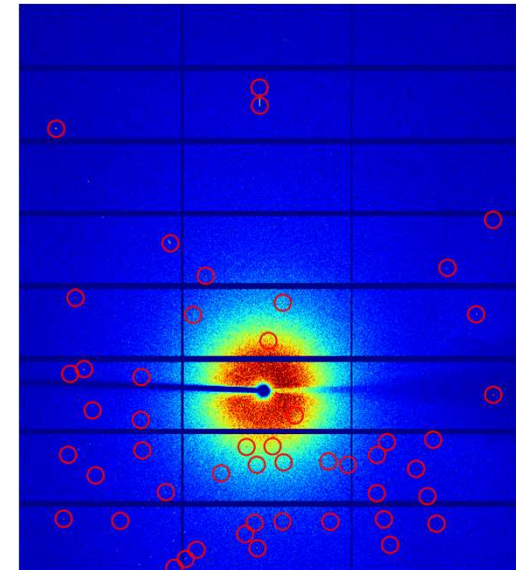
# Orientation matrix search

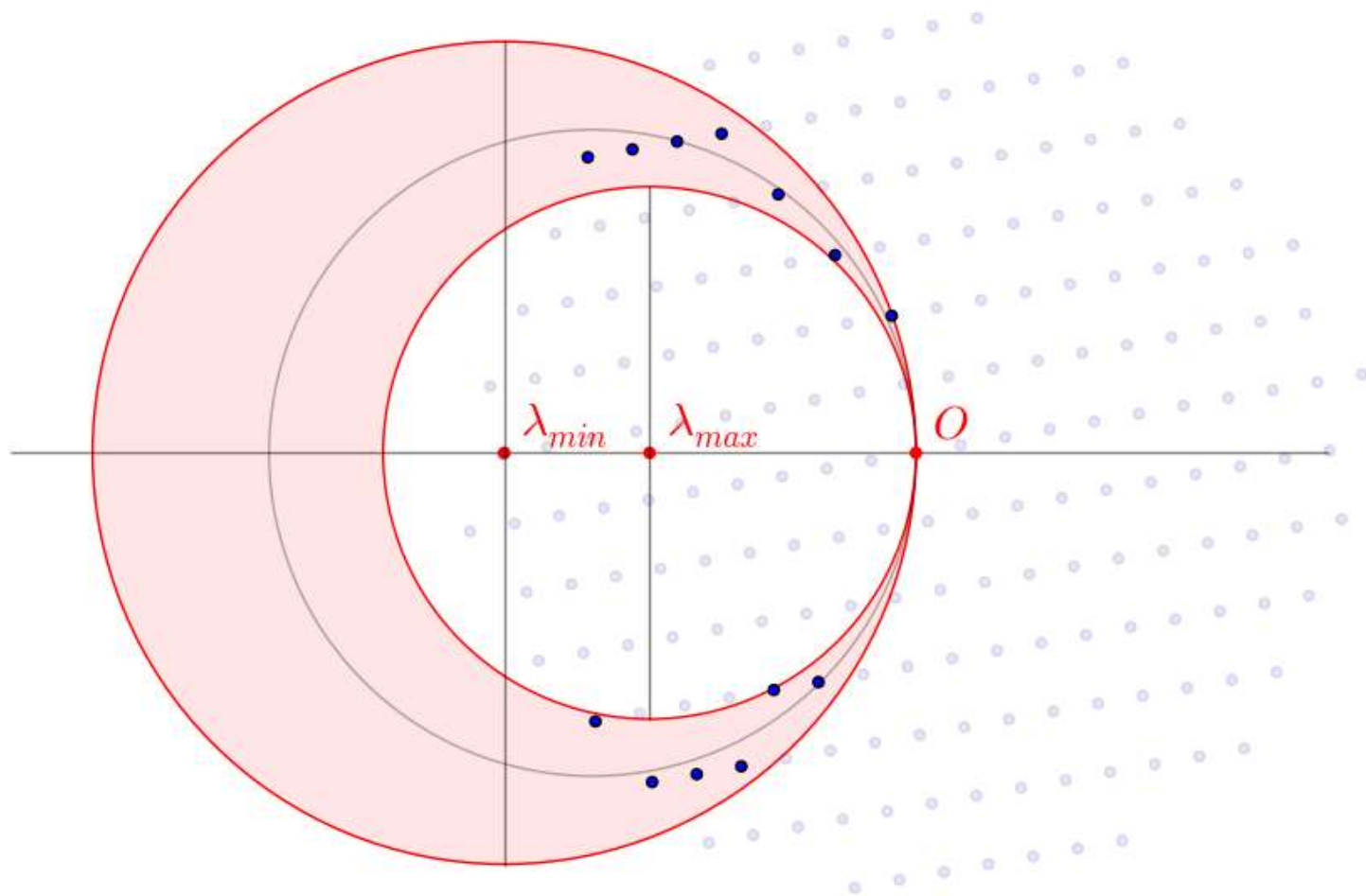
ZSM-5	20.0022
<i>Pnma</i>	19.8990
	13.3830



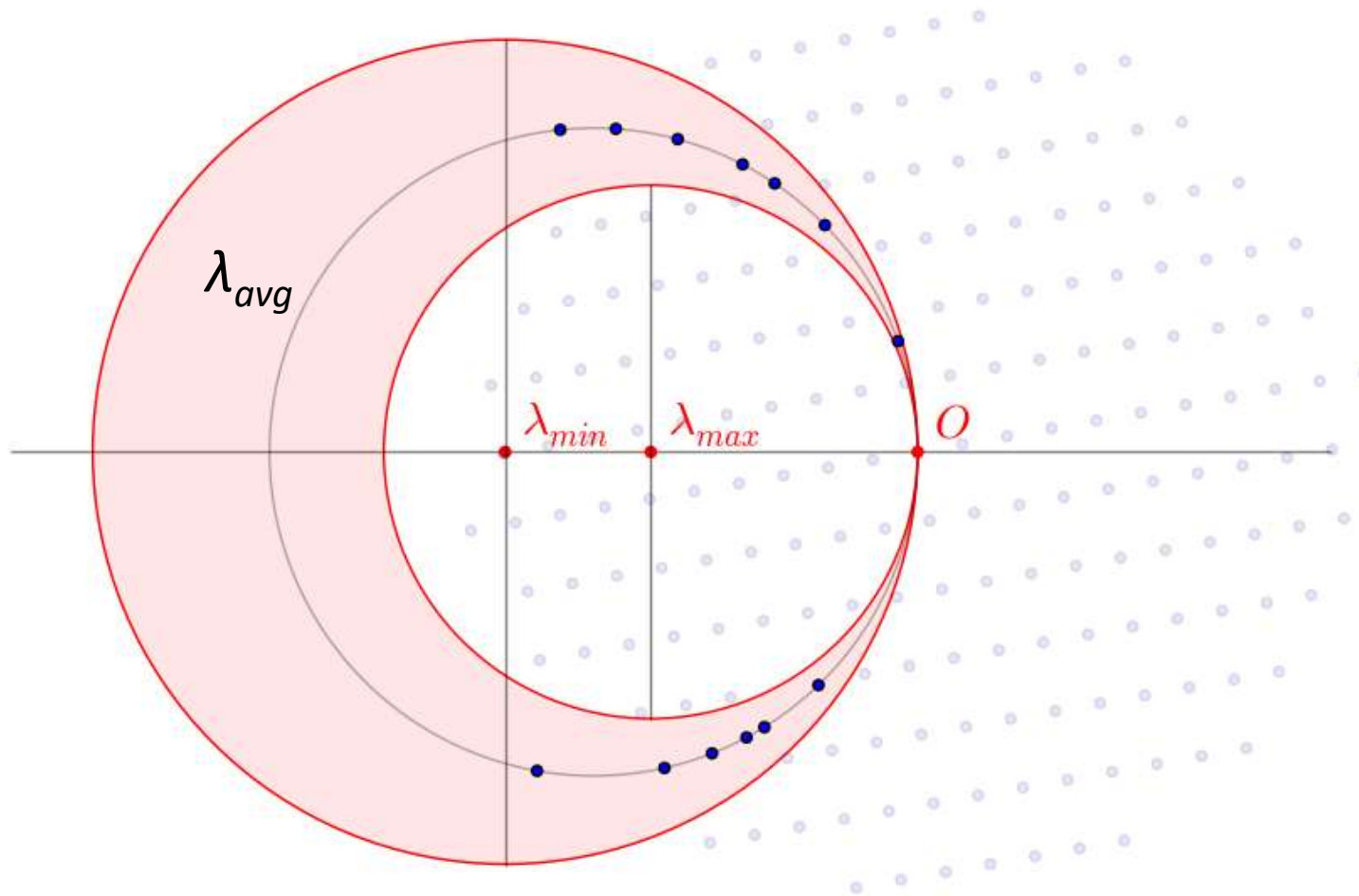
# Typical run (ZSM-5)

- 58 peaks in frame, take 10 peaks with lowest  $2\theta$  angle
- 45048 potential reflection pairs
  - Reject pairs with wrong angles
- 1943 valid orientation matrices
  - Perform least-squares optimization of rotation matrix
  - Assign wavelengths

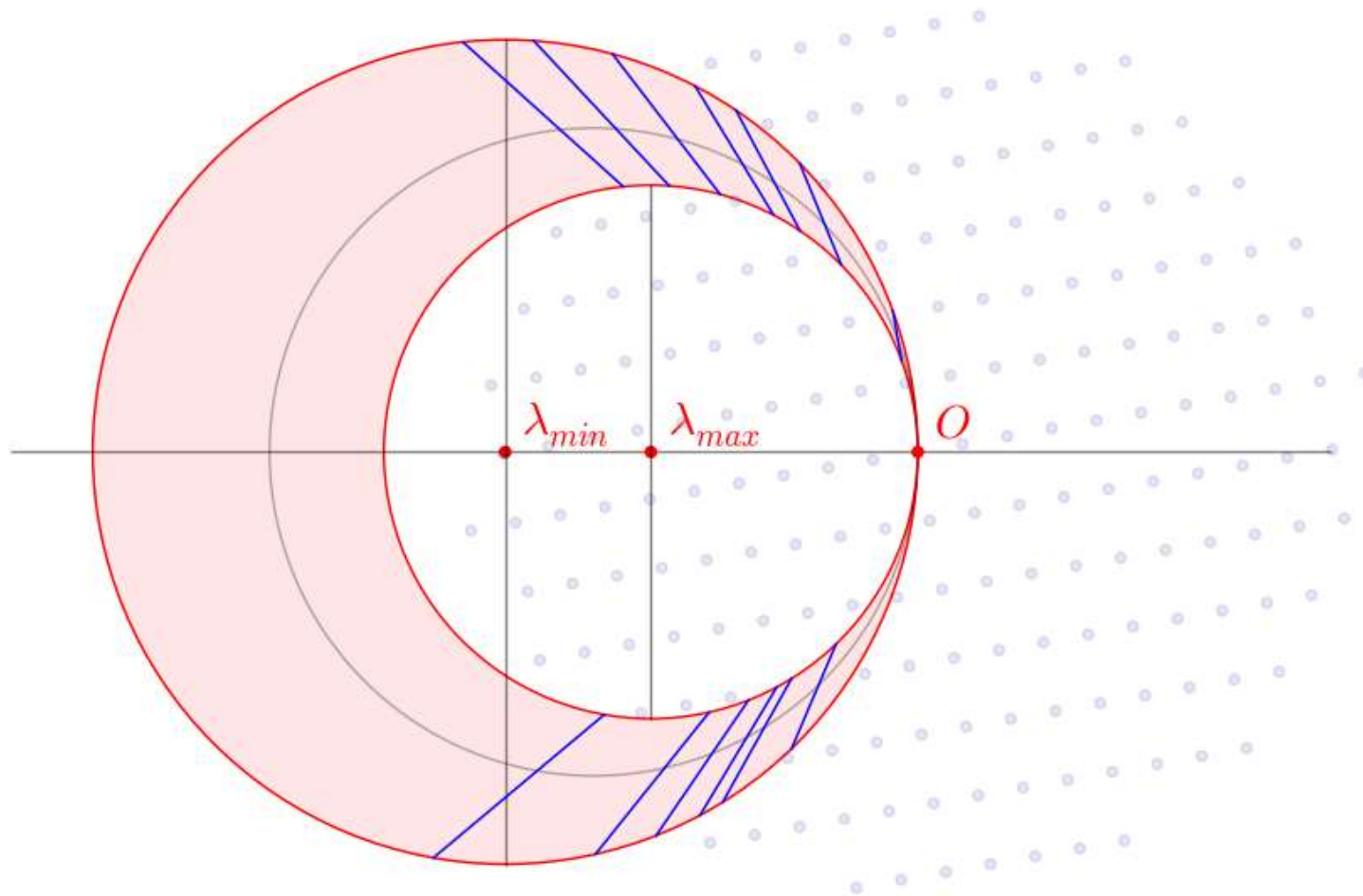






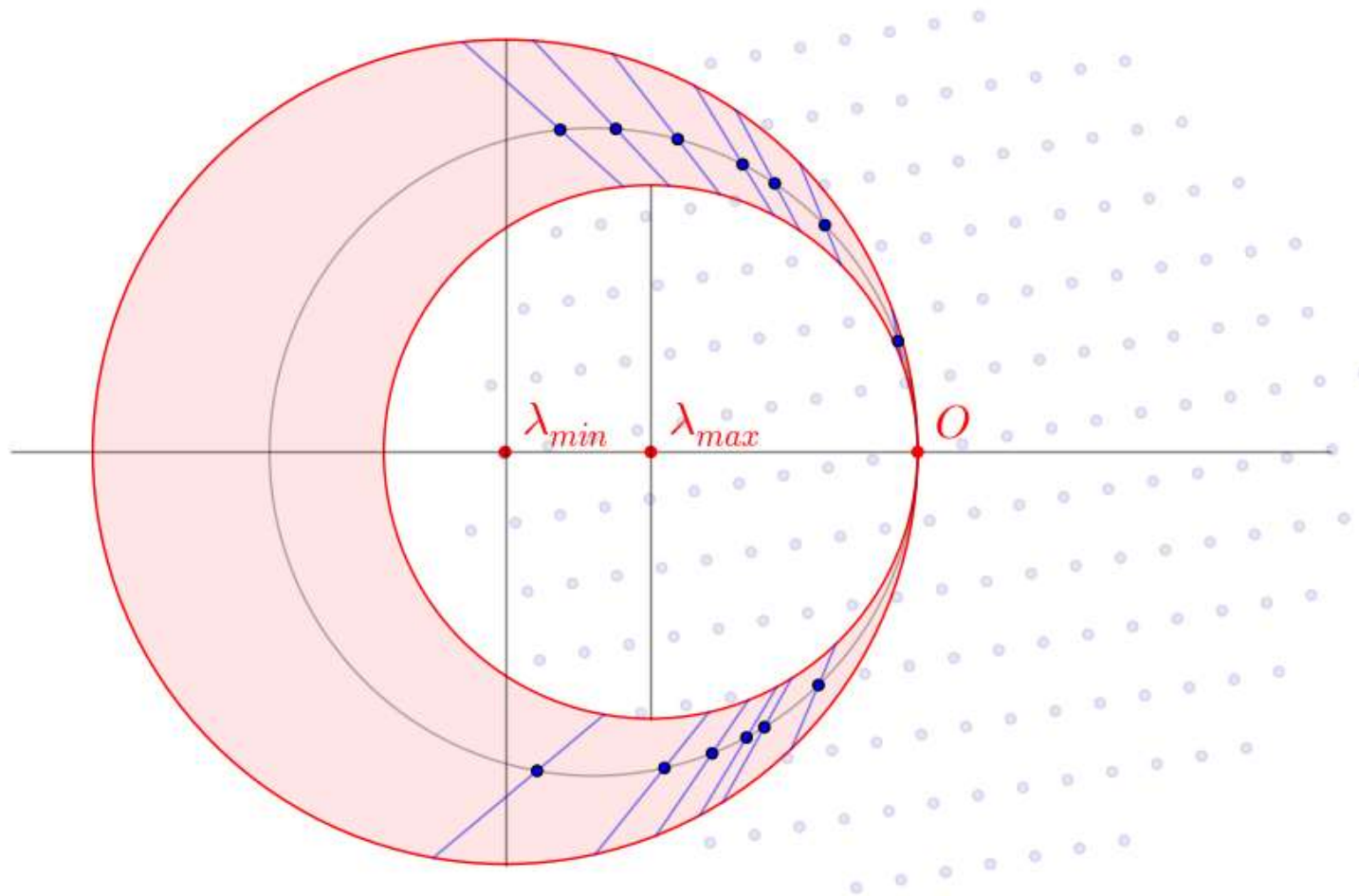


Assume monochromatic radiation ( $\lambda_{avg} = \frac{1}{2}[\lambda_{min} + \lambda_{max}]$ )  
 Find orientation matrix

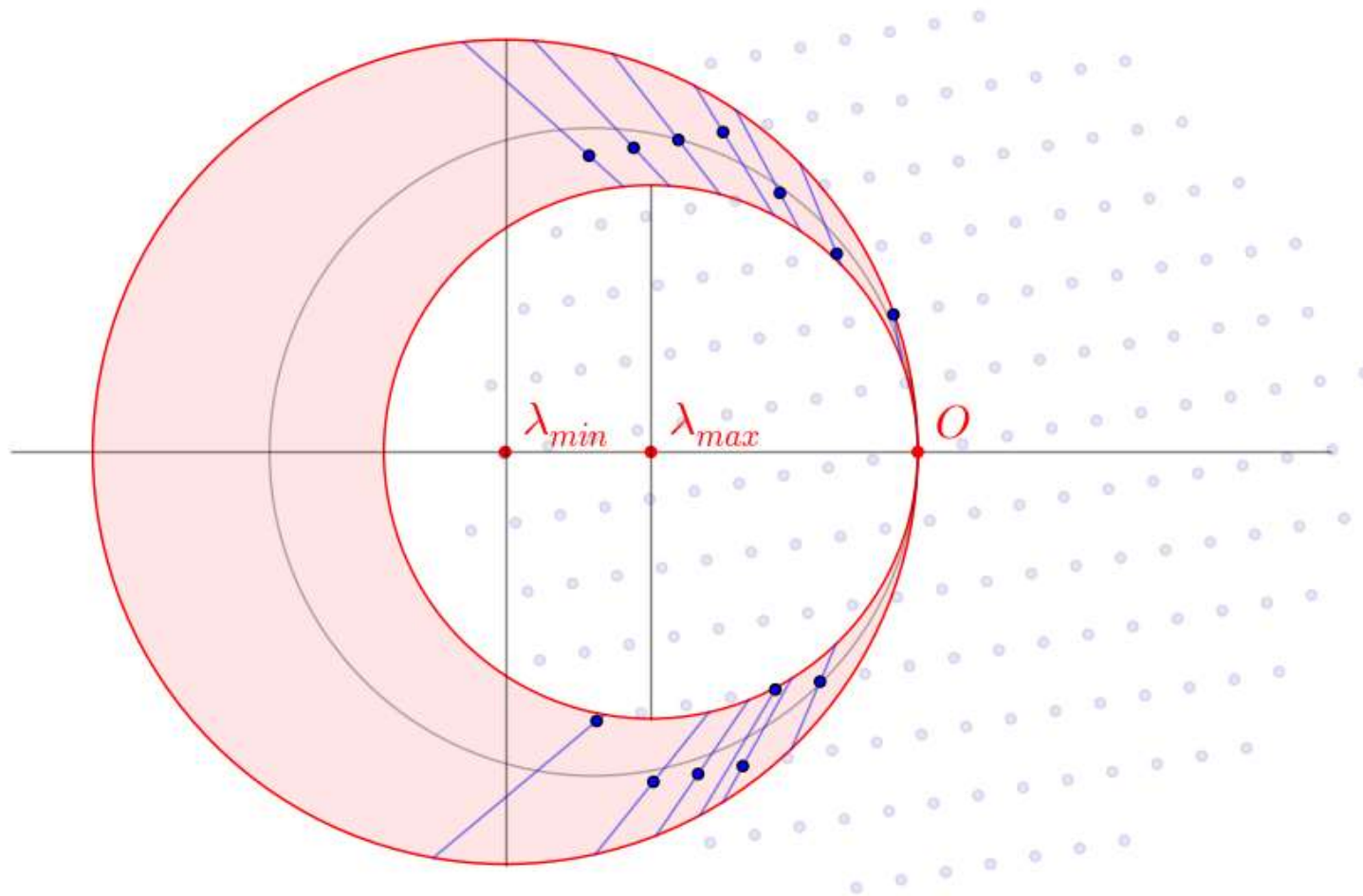


Reflection wavelength indeterminate

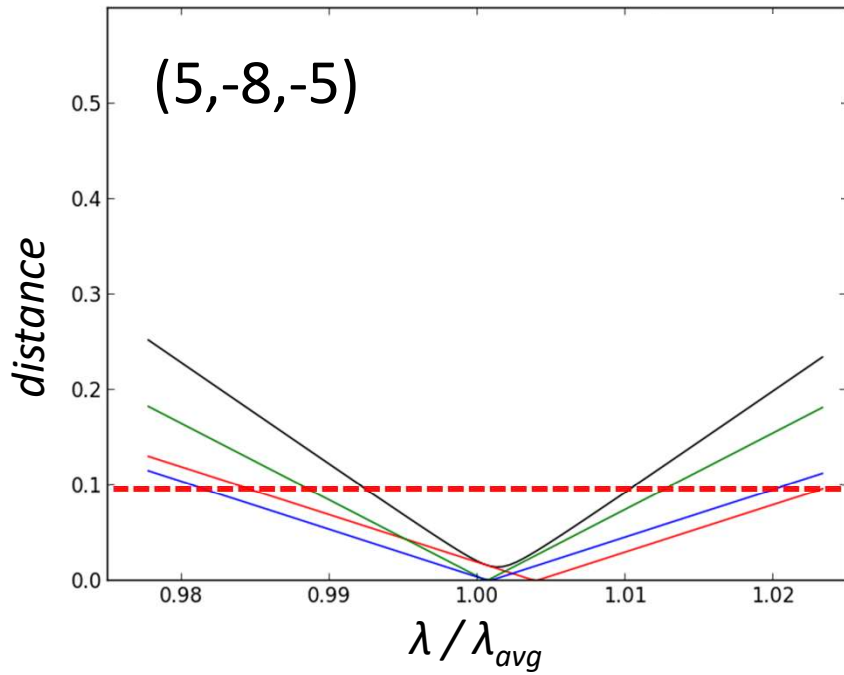




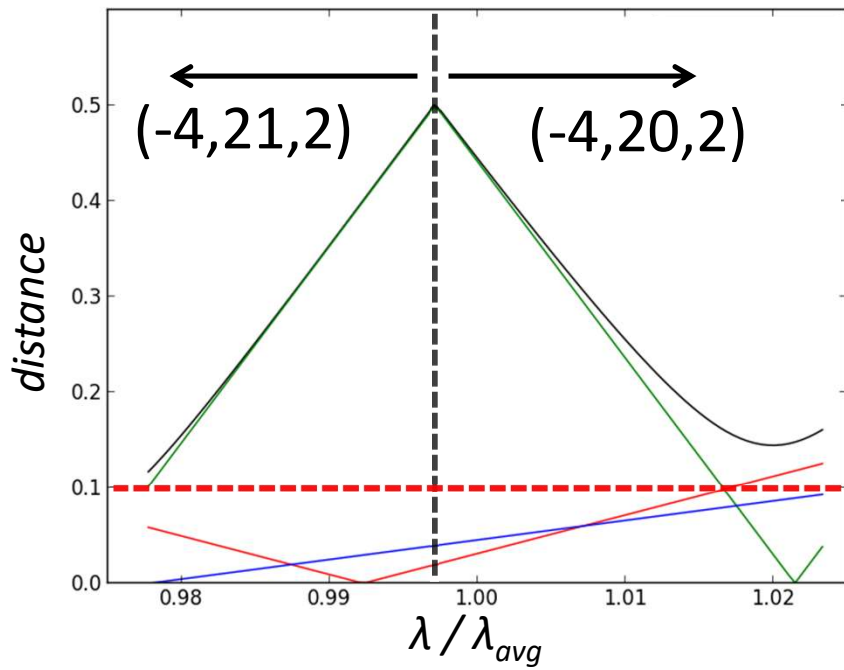
Allow reflection to *slide* along  $\mathbf{q}$ -vector



Minimize distance to integer index  
Retrieve wavelength



— Total difference  
 —  $h_{diff}$   
 —  $K_{diff}$   
 —  $l_{diff}$

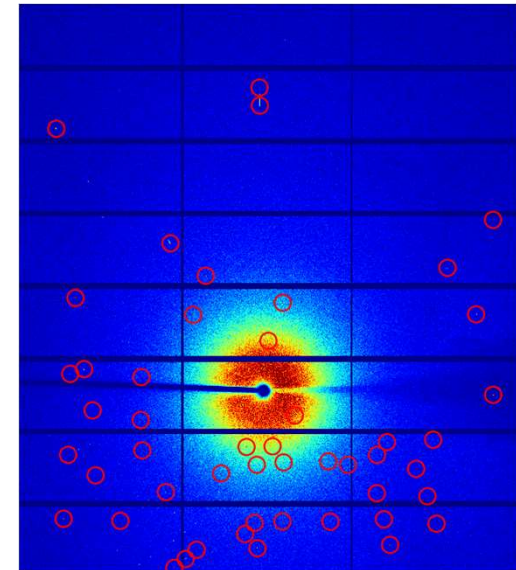


Threshold = 0.1  $\longrightarrow$ 

- Calculate  $N_{fit}$
- Calculate *score*

# Typical run (ZSM-5)

- 58 peaks in frame, take 10 refs with lowest  $2\theta$  angle
- 45048 potential reflection pairs
  - Reject pairs with wrong angles
- 1943 valid orientation matrices
  - Perform least-squares optimization of rotation matrix
  - Assign wavelengths
- 44 solutions with  $n_{fit} > 25$ 
  - merge symmetry equivalent / duplicates
- 2 unique solutions
  - Remove sys. absences
- Pick best solution!



	$n_{fit}$	score
solution 1	55	0.1517
solution 2	52	0.2671

Unit cell known  
Start with  $\mathbf{q}$ -vectors  
Assume average wavelength ( $\pm 2\%$ )

# Approach to indexing

## Generation

Generate candidate orientation matrices

1. Orientation matrix search

Map  $d$ -spacings to potential indices  
Use peak pairs

2. "Brute force" approach

Calculate all possible orientations  
(1.5 million)



## Evaluation

Select good candidate(s)  
(number of indexed peaks  $N_{fit}$ )



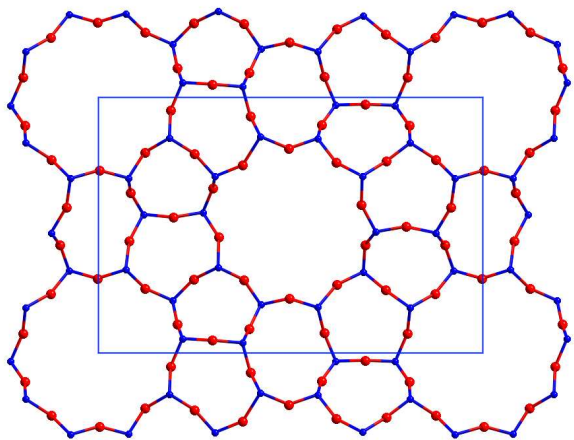
Assign wavelength & calculate score  
Ranked by  $score/N_{fit}^2$



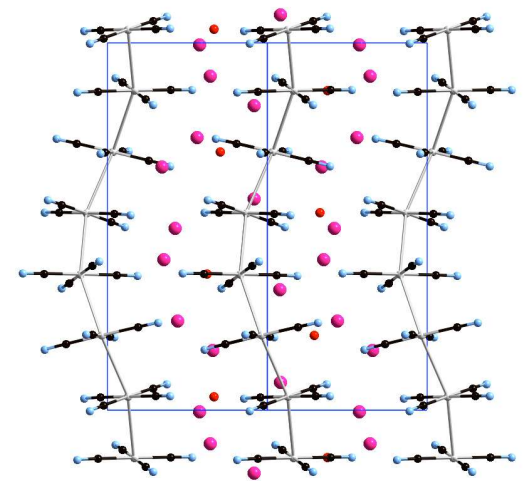
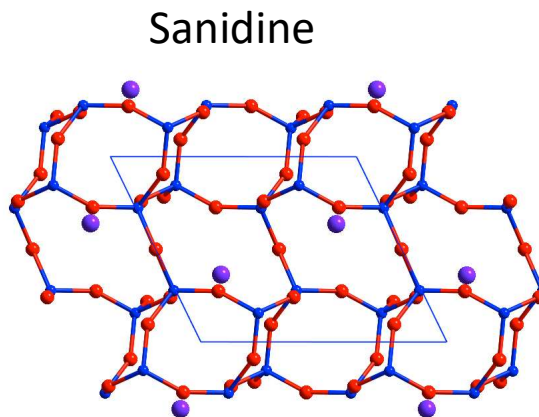
Greedy set optimization routine  
(Multiple crystals only)

# Test samples

	Space group	<i>a</i>	<i>b</i>	<i>c</i>	$\beta$
ZSM-5	<i>Pnma</i>	20.0022	19.8990	13.3830	
Sanidine	<i>C2/m</i>	8.5832	13.0076	7.1943	116.023
$\text{Cs}_2[\text{Pt}(\text{CN})_4]\cdot\text{H}_2\text{O}$	<i>P6_5</i>	9.7910		19.5100	



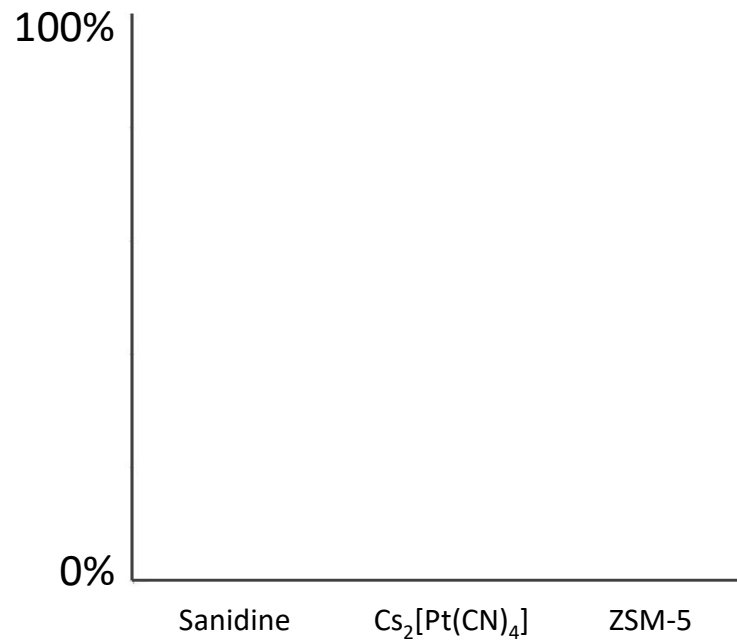
ZSM-5



$\text{Cs}_2[\text{Pt}(\text{CN})_4]\cdot\text{H}_2\text{O}$

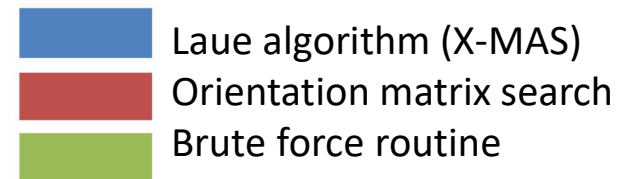
# Tests with 1 crystal in the beam

Indexing  
success rate  
(crystals per  
frame)



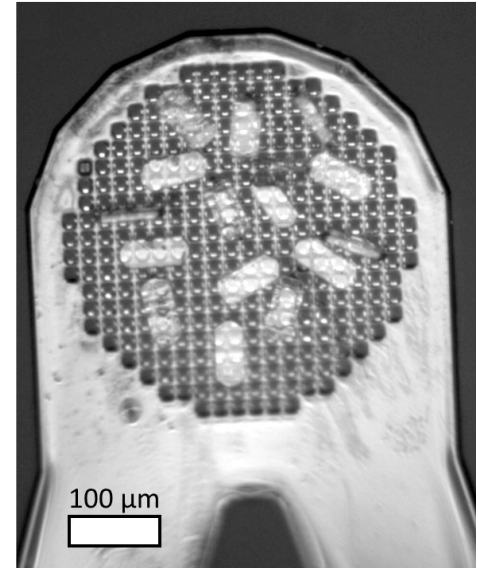
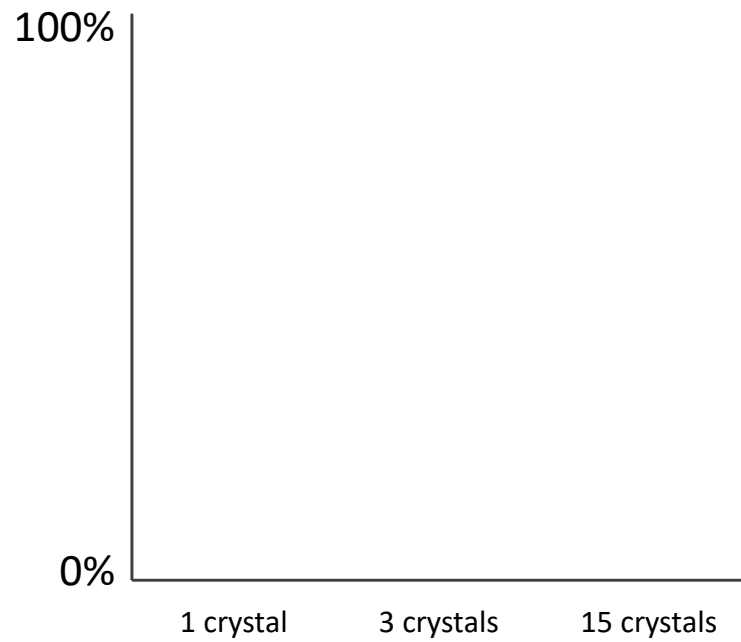
Total frames: 360  
SNBL (ESRF),  $\varphi$ -scan, 1° / step  
4.6% bandwidth

Time per frame



# Tests with multiple crystals in the beam (ZSM-5)

Indexing success rate (crystals per frame)



15 crystals

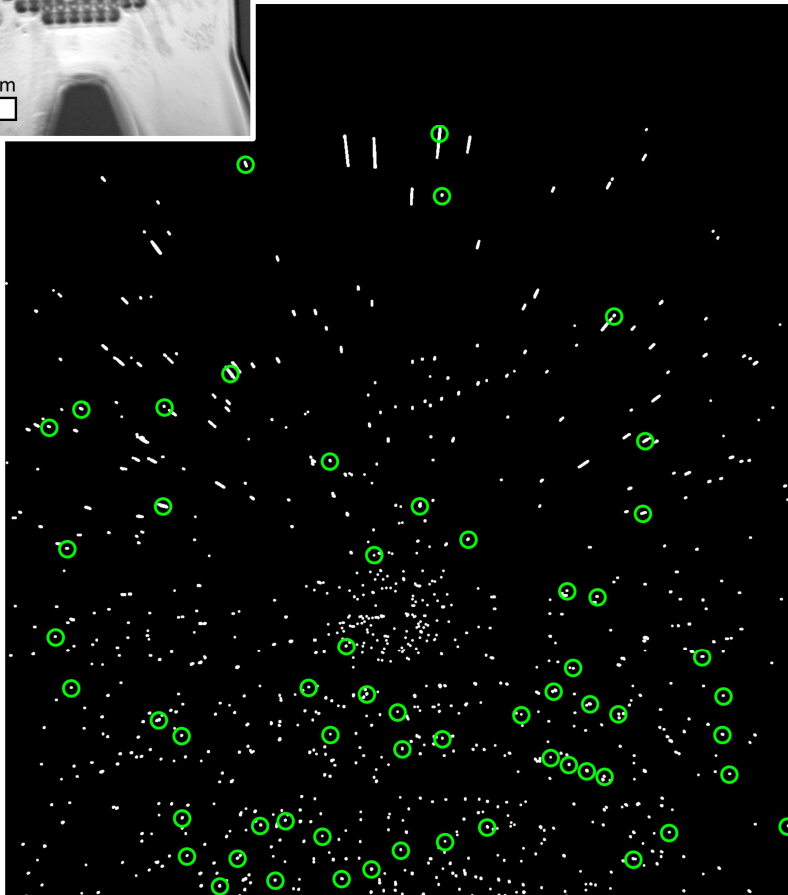
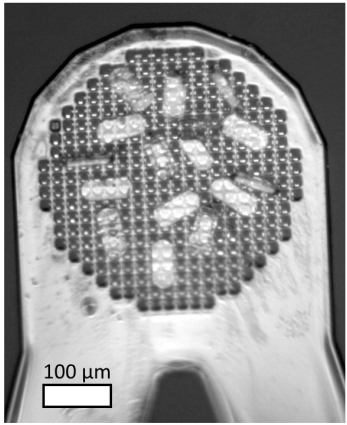
Time per frame



- Laue algorithm (X-MAS)
- Orientation matrix search
- Brute force routine

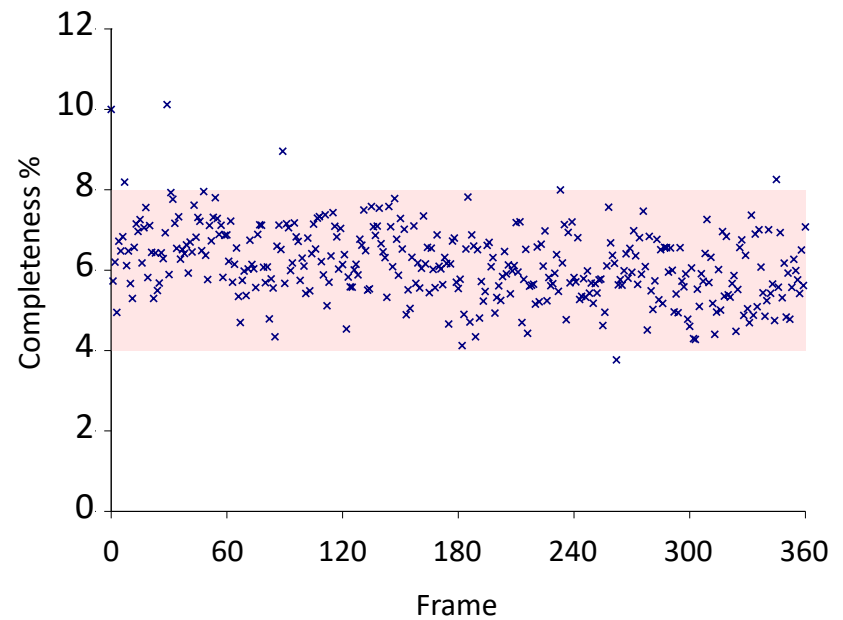


# Multi-crystal indexing (ZSM-5)

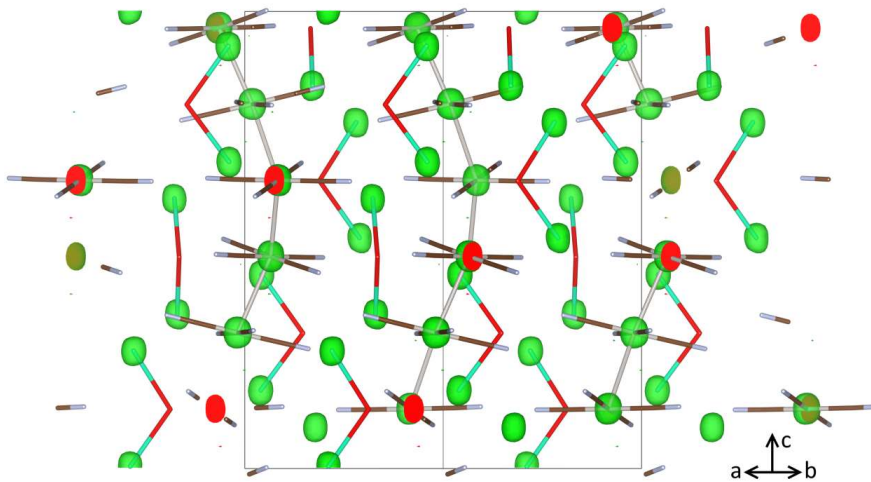


1/15 crystals → 57/595 reflections

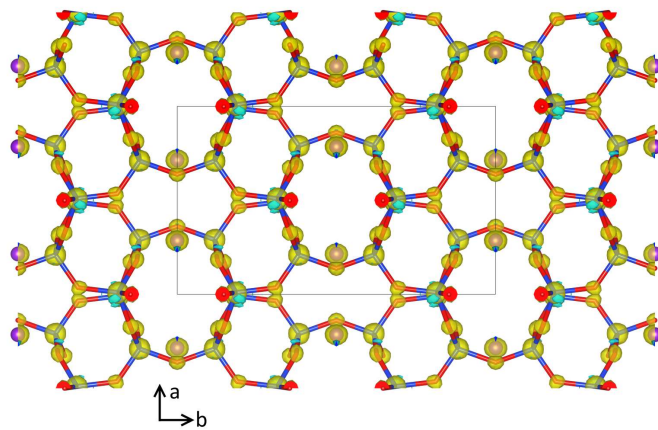
	No. crystals	Avg. No.	Completeness
1 crystal	351	1	0.8%
3 crystals	902	2.8	1.5%
15 crystals	2854	8.5	6.0%



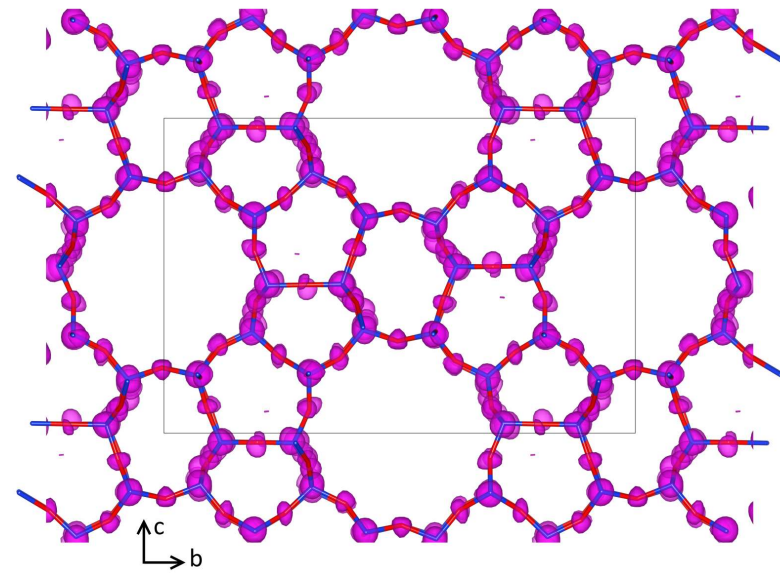
# Structure solution (Charge flipping)



$\text{Cs}_2[\text{Pt}(\text{CN})_4] \cdot \text{H}_2\text{O}$



Sanidine



ZSM-5

# Conclusions

- Single snapshots can be indexed reliably
  - Useful data can be extracted from nearly every frame
- Up to 11 crystals can be indexed in a single frame
  - Multiple crystals in the beam is an advantage!
- Algorithms work with any data <5% bandwidth
- Challenges
  - *Ab initio* indexing
  - Scaling
  - Merging
- Applications
  - Structure determination of complex/beam sensitive materials (SwissFEL)
  - *In-situ/time-resolved* experiments